A New Recursive Algorithm for Universal Coding of Integers

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Received: 14/Jul/2013

Revised: 08/Sep/2014

Accepted: 13/Nov/2014

Abstract

In this paper, we aim to encode the set of all positive integers so that the codewords not only be uniquely decodable but also be an instantaneous set of binary sequences. Elias introduces three recursive algorithms for universal coding of positive integers where each codeword contains binary representation of the integer plus an attachment portion that gives some information about the first part [1]. On the other hand, Fibonacci coding which is based on Fibonacci numbers is also introduced by Apostolico and Fraenkel for coding of integers [2]. In this paper, we propose a new lossless recursive algorithm for universal coding of positive integers based on both recursive algorithms and Fibonacci coding scheme without using any knowledge about the source statistics [3]. The coding schemes which don't use the source statistics is called universal coding, in these universal coding and decoding schemes assign binary streams to positive integers and conversely, without any need of use to probability masses over positive integers. We show that if we use Fibonacci coding in the first part of each codeword we can achieve shorter expected codeword length than Elias Omega code. In addition, our proposed algorithm has low complexity of encoding and decoding procedures.

Keywords: Universal Source Coding (data compression); Fibonacci Coding; Elias Coding Schemes; Integer Representation; Omega Coding; Redundancy.

1. Introduction

Researchers in the field of source coding and data compression have focused on offering efficient and fast running algorithms that have simple software and hardware implementation with expected codeword length close to entropy [4]. In this work, we aim to encode all the positive integers so that the set of codewords not only be uniquely decodable but also be an instantaneous set of binary sequences [5]. There are many situations in which the alphabet is a set of positive integers. For example, we might have a list of items and we wish to encode the position of an element in the list. Also, we may want to encode an image file by encoding the intensities.

We can classify algorithms in this field into two categories: In the first one, that we refer to as recursive algorithms, codewords have a prefix portion or a suffix portion of binary string that converts standard binary representation of positive integers to a uniquely decipherable presentation or even an instantaneous representation with minimum possible expected codeword length and low complexity encoding and decoding algorithms. In the second category, there are algorithms based on applying a complex mathematical method to compress equivalent binary representation of positive integers as much as possible. It is obvious that, with the same goal of getting shorter expected codeword length, algorithms in the second category have more complexity for encoding and decoding procedures compared with the algorithms in the first category.

Peter Elias offers three universal coding schemes to encode positive integers [1]. Universal coding means that there is no need to use the probability distribution or statistical properties of the source that we want to encode or the data that we want to compress. Elias named these three algorithms Gamma, Delta and Omega representations. Usually compared with Delta, Omega, ω , has shorter expected codeword length while Delta has shorter expected codeword length compared with Gamma. These three algorithms are in the first category; they attach a binary representation to standard binary presentation of the positive integer that provides the capability of being uniquely decipherable or instantaneous property to the codeword set [5]. Our proposed algorithm is also in the category of recursive schemes.

In Omega coding scheme for positive integers [1], first the binary representation of the integer is obtained. Then, we attach a prefix portion that shows the number of bits that was written in the previous step minus one in a binary format. We continue this procedure until the prefix portion be two-bit size part. At the end of the procedure, bit "0" is attached as a delimiter to indicate the end of the codeword. For example, the Omega codeword for 2012 is

$\omega(2012) = 111010111110111000$

Mathematically, Elias Omega codeword for any positive integer n_0 can be written as the following recursive structure [1], [6]

$$C_E(n_0) = [n_k]_2 [n_{k-1}]_2 \dots [n_1]_2 [n_0]_2 0 \tag{1}$$

Where $[n]_2$ is the binary representation of n. Each n_k in (1) is obtained recursively by $n_k = \lfloor \log_2 n_{k-1} \rfloor$ where the recursive algorithm stops when the length of $[n_k]_2$ is two. The decoding procedure is simply the inverse of the encoding procedure: we read the first two bits of every codeword $C_E(n_0)$ to obtain n_k , and then we know that $n_k + 1$ represents the bit length of $[n_{k-1}]_2$. Thus the length of $[n_{k-1}]_2$ is recursively obtained from n_k . We continue this procedure until the first bit of the next portion is 0, and then the last portion is the number that is encoded. In fact, since the most significant bit (MSB) of every $[n_k]_2$ is "1", delimiter "0" can stop the recursion and n_0 can be easily found.

A simple coding scheme in the second category of algorithms is Fibonacci coding to encode positive integers [2], [7]. In this scheme, we write an integer number according to summation of Fibonacci numbers. The first 10 Fibonacci numbers, F_n for $n = 1, 2, \dots, 10$, are shown in Table 1. To encode an integerN, first the largest Fibonacci number equal to or less than N is determined. If the number subtracted was the i'th Fibonacci number, F_i , a "1" will be placed as the i'th bit in the codeword. By subtracting this Fibonacci number from N, we repeat the previous steps for the reminder untila remainder of 0 is reached. Eventually, we add a "1" tothe rightmost digit in the codeword, which indicates the codeword is ended. The Fibonacci representation of an integer has an interesting property that it does not contain any adjacent 1's [8], so that receiving "11" string means the end of the codeword [2],[7]. For example, the Fibonacci codeword of 2012 is

F(2012) = 10100001000010011,

Since $2012 = F_1 + F_3 + F_8 + F_{13} + F_{16}$, in which F_i shows the i'th term in Fibonacci sequence. A disadvantage of the Fibonacci coding is that the complexity of coding and decoding algorithms increases by increasing the numbers to be coded or the length of stream to be decoded but this scheme is very efficient if larger numbers are more frequent than smaller ones [9].

Table 1: Fibonacci Numbers

$F_1 = 1, F_2 = 2,$	$F_n = F_{n-1} + F_{n-2}$	$\forall n \geq 3$
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F_1	F_2	F_3	F_4	F_5	F_6	F_7	F_8	F_9	F_{10}
1	2	3	5	8	13	21	34	55	89

In this paper, we propose a new recursive algorithm to encode all of the positive integers. In this proposed coding scheme, every codeword has a prefix portion which provides the uniquely decipherable property to the codeword set. We observe that our proposed algorithm is an instantaneous set of binary codes with low complexity of encoding and decoding procedures (in both software and hardware implementations). Numerical simulations show that generally for most of probability distributions, the proposed coding has shorter expected codeword length that Elias Omega coding scheme in [1].

The paper is organized as follows. The problem definition is presented in Section 2. Our proposed universal coding for positive integers is introduced in Section 3. For comparison, the expected codeword length of our proposed algorithm is compared with that of the Elias ω code in Section 4, where two sufficient conditions on the discrete probability distribution of the input source are provided in order to get shorter expected codeword length than Omega coding. We present the decoding procedure in Section 6.

2. Problem Definition

The general problem we encounter here is encoding the set of integer numbers without any use of probability distribution. In other words, the encoder and the decoder do not know the statistics of the input stream. This is called universal source coding or universal data compression [10]. The concept of universal coding of integers gets a lot of attention by researchers who work in source coding and data compression field [3].

Similar to [1], [6], [11]-[13] we have treated the universal coding of the positive integers that have decreasing probability distribution for positive integers, i.e.,

$$P(n) \ge P(n+1) \quad \forall n \in \mathbb{N}$$

where P(n) is a probability distribution on the set of positive integers, $\mathbb{N} = \{1, 2, 3, \dots\}$. We assume that the inputsymbols are emitted by a memoryless information source with a possibly infinite alphabet, i.e., data emitted from the source is an independent and identically distributed (i.i.d) stream. Since we assume that the source has infinite alphabet, we can apply a one-to-one mapping between the source alphabet and the set of positive integers.

We aim to provide an encoding algorithm that encodes all the positive integers independently. Thus, the encoder is a memoryless system. Note that there are some universal encoding schemes in the literature which use memory in the encoding procedures [14]-[16].

By considering integers of the source output into blocks, each one containing n integer numbers, we can apply our algorithm to each block separately, similar to thescheme in [17]. From the decreasing probability distribution for integers, it is clear that the codeword length would be an ascending function of n. Our goal is to encode positive integers with low complexity and minimum redundancy. Note that for a probability distribution P, the normalized redundancy is defined in [18] as

$$R(P) \triangleq \frac{\mathbb{E}L(P) - H(P)}{H(P)}$$

where $\mathbb{E}L(P)$ is the expected codeword length over the probability distribution P, and H(P) denotes the entropy of the source. Due to first theorem of Shannon [5], we know that $R(P) \ge 0$, so we get more efficient compression if the normalized redundancy approaches to zero. Although there are some schemes that achieve an expected codeword length close to the Shannon entropy over most of probability distributions [19], [20], the drawback of these algorithms is being lossy. In this paper, we describe a lossless scheme that encodes positive integers universally with expected codeword length close to the entropy of the source due to Elias Omega codeword length [1].

3. Proposed Coding Scheme

Here, we describe our proposed algorithm. As we mentioned before, our algorithm is a recursive scheme which has three steps:

- 1. First, we write the standard binary representation of the positive integer number that we intend to encode and remove its most significant bit. For instance, for integer 17, we write 0001.
- 2. Then, we count the number of bits that we obtained in the first step (clearly, for number n we have $\lfloor \log_2 n \rfloor$ bits). For the integer number 17, we have 4 bits.
- 3. Finally, we attach the Fibonacci code of $\lfloor \log_2 n \rfloor$ to the left side of the binary string we obtained in the first step.

As an example, the integer number 17 has 4 bits in the first step and hence the Fibonacci codeword for integer 4 is F(4) = 1011. We attach 1011 to the left side of 0001 and obtain the codeword 10110001.

However, there exists one problem here. In the above algorithm, the positive integer "1" does not have any codeword. In other words, this algorithm produces the null codeword for the number "1", so we have to assign a single bit to determine the number to be encoded is "1" or not. We add a single bit at the frontier of the codewords to determine whether the number that is encoded is "1" or not. At the decoder, if the first bit is 1 we know that "1" is encoded and if the first bit is 0 we conclude that the encoded number is not "1". So that the codeword of "1" is the single bit 1, i.e., we write C(1) = 1. As a result, the codeword for the positive integer number 17 is C(17) = 010110001 where we added single "0" bit to the beginning of the codeword "10110001".

In Table 2, we provide the codewords of some positive integers based on our proposed scheme.

Integer number	Our codeword
1	1
9	00011001
23	010110111
53	00001110101
78	010011001110
1000	0100011111101000
2012	00100111111011100

Table 2: Codewords of some integers based on our proposed scheme

4. Performance Comparison between our Proposed Scheme and Omega Scheme

For comparison, the codeword lengths of the proposed scheme for some integers versus Elias ω code, which is a verystrong andfamous method in data compression and algorithmic source coding, are provided in Table 3. Based on the codeword lengths in Table 3 and also using simulation results, we observe that the only integers for which our codeword lengths exceed Elias ω codeword lengths are {2,3,8,9,10,11,12,13,14,15} (among all of the positive integers) and for the rest of integers, {1, 4, 5, 6, 7, 16, 17, 18, ...}, our coding scheme performs superior to Elias ω coding scheme, i.e., our codewords have shorter lengths than Elias ω codewords. Thus, our proposed algorithm results in a shorter expected codeword length over the most of discrete probability distributions, compared with the Elias ω coding scheme.

An advantage of our proposed algorithm is that if there is no integer "1" in the input sequence, we can eliminate the first bit from all of the code words, since this bit is determining whether the encoded number is "1" or not.

We apply our proposed algorithm to encode all the integers between "1 to 128". In Figure 1, we presented codeword lengths of two coding schemes: our proposed coding scheme and Elias Omega coding scheme. We observe that except for some small integers, our codeword lengths are shorter than codeword lengths of Elias ω coding scheme. More precisely, the only integers that Omega codewords have shorter lengths are 2,3,8,9,10,11,12,13,14 and 15 among all the positive integers and for the rest of integers $(\{1,4,5,6,7,16,17,18,...\})$ our codewords have shorter lengths.

Integer number	Elias code	Our proposed code
1	1	1
2-3	3	4
4-7	6	6
8-15	7	8
16-31	11	9
32-63	12	11
64-127	13	12
128-255	14	13

 Table 3: Codeword length of our proposed scheme

 v.s Elias
 coding scheme

Also note that because of constructing the prefix portion of the codeword from number of bits that is written in the first step of the encoding, the codeword lengths differ for integer numbers that are different powers of 2. In other words, for every positive integerk, all of the integers from 2^{k-1} to $2^k - 1$ have equal codeword length, which can be observed in Figure 1.



Fig. 1: Performance of our proposed algorithm compared with that of Elias Omega coding scheme.

In the next two Theorems, we provide strong sufficient conditions for discrete probability distributions over integers for which our proposed algorithm performs superior to the other algorithms such as Elias Omega coding scheme.

Theorem 1. A strong sufficient condition on the discrete probability distribution of a source to achieve shorter expected codeword length, based on our algorithm, than Omega coding scheme is

$$2(p_{16} + p_{17} + \dots + p_{31}) \\ \ge (p_2 + p_3) \\ + (p_8 + p_9 + \dots + p_{15})$$
(2)

where p_i denotes the occurrence probability of number "*i*" in the output sequence of the discrete source. **Proof:** From the condition provided in Theorem 1, if we add the following terms to both sides of (2):

$$p_1, \exists (p_2 + p_3), 6(p_4 + \dots + p_7), 7(p_8 + \dots + p_{15}), 9(p_{16} + \dots + p_{31}),$$

we obtain

$$p_{1} + 3(p_{2} + p_{3}) + 6(p_{4} + \dots + p_{7}) + 7(p_{8} + \dots + p_{15}) + 11(p_{16} + \dots + p_{31})$$

$$\geq p_{1} + 4(p_{2} + p_{3}) + 6(p_{4} + \dots + p_{7}) + 3(p_{8} + \dots + p_{15}) + 9(p_{16} + \dots + p_{31}).$$

Let $L(\omega(n))$ and L(C(n)) denote the codeword lengths for the Elias Omega code and our proposed code, respectively. Since based on Table 3, we know that for the positive integers larger than "32", the codeword lengths of our proposed scheme are shorter than those of Elias ω code, we can write the following inequality

. ...

$$p_{1} + 3(p_{2} + p_{3}) + 6(p_{4} + \dots + p_{7}) + 7(p_{8} + \dots + p_{15}) + 11(p_{16} + \dots + p_{31}) + \sum_{j=32}^{\infty} p_{j}L(\omega(j)) > p_{1} + 4(p_{2} + p_{3}) + 6(p_{4} + \dots + p_{7}) + 8(p_{8} + \dots + p_{15}) + 9(p_{16} + \dots + p_{31}) + \sum_{j=32}^{\infty} p_{j}L(C(j))$$
(3)

If $\mathbb{E}[.]$ denotes the expectation of a random variable over the probability distribution of the source, then (3) results in

$$\mathbb{E}[L(\omega(n))] > E[L(C(n))].$$

Thus, we achieve a code whose expected codeword length is shorter than that of Elias coding scheme. This completes the proof.

For example, if we check the condition of Theorem 1, given in (2), for character probability distribution (relative frequencies of letters in the English language [21]) we observe that

$$2(p_{16} + p_{17} + \dots + p_{31}) = 0.3895,$$

$$(p_2 + p_3) + (p_8 + p_9 + \dots + p_{15}) = 0.379,$$

which shows validity of the condition in Theorem 1 for a practical scenario.

Theorem 2. The second strong sufficient condition on the discrete probability distribution of a source to achieve shorter expected codeword length, based on our coding scheme, than Omega coding is

$$p_{16} + p_{17} + p_{18} + \cdots \\ \ge (p_2 + p_3) \\ + (p_8 + p_9 + \cdots + p_{15})$$
(4)

where p_i denotes the occurrence probability of number "*i*" in the output sequence of the discrete source.

Proof: Using (4) and adding the following terms to both sides:

$$p_1, p_2 + p_3, p_4 + \dots + p_7, p_8 + \dots + p_{15},$$

we get

$$1 = p_1 + p_2 + p_3 + \cdots$$

$$\geq p_1 + 2(p_2 + p_3) + p_4 + \cdots + p_7$$

$$+ 2(p_8 + \cdots + p_{15})$$
(5)

Since we know that our codewords have one bit more than Elias ω coding scheme only for the following positive integers: {2,3,8,9,10,11,12,13,14,15}, and for the rest of integers, our scheme has shorter codeword length compared with the Omega coding scheme, we can write (5) as

$$p_1 + 3(p_2 + p_3) + 6(p_4 + \dots + p_7) + 7(p_8 + \dots + p_{15}) + 11(p_{16} + \dots + p_{31}) + \sum_{j=32}^{\infty} p_j L(\omega(j)) > p_1 + 4(p_2 + p_3) + 6(p_4 + \dots + p_7) + 8(p_8 + \dots + p_{15}) + 9(p_{16} + \dots + p_{31}) + \sum_{j=32}^{\infty} p_j L(C(j))$$

which results in

$$\mathbb{E}[L(\omega(n))] > E[L(C(n))].$$

Thus, the proof is complete.

5. Decoding Procedure

Decoding scheme of a universal source code also should be universal, which means that the decoder does not know the source statistics [22].

By assuming an ideal communication channel with no error, the decoding algorithm can be described as follows:

From the first bit of the codeword, the decoder knows that the coded number is "1" or not. In other words, if the MSB of the received codeword is 1, the integer number that is encoded is "1", otherwise the integer number that is encoded is not "1". In the latter case, the decoder reads the remaining part of the codeword until it receives the first "11" substring. This last part is the Fibonacci portion of the codeword. By decoding this Fibonacci portion and assuming that it is decoded to the integer number $\log_2 n$, the decoder then reads $\log_2 n$ bits after "11" sequence. This part with adding "1" as its MSB will be the binary presentation of the number that has been encoded.

For example, if we receive the following sequence: 110101100011, by applying the decoding scheme presented here we obtain the following sequence of integers: "1-1-17-1".

6. Conclusions

In this paper, we proposed a new recursive algorithm that achieves an expected codeword length which is shorter than that of other universal coding schemes such as Elias ω coding scheme. Note that Elias ω coding scheme has the shortest expected codeword length among all three coding schemes presented in [1]. In the proposed algorithm, we applied Fibonacci coding scheme in the prefix part of the codeword. More precisely, we first obtain the standard binary representation of the positive integer number and remove its most significant bit. Then, we count the number of bits that we obtained in the first step. We then attach the Fibonacci code of the number of bits obtained in the first step to the left side of the binary string we obtained in the first step. We know that the Fibonacci representation of an integer has the interesting property that it does not contain any adjacent 1's, so that receiving "11" string means the end of prefix part. Moreover, here we provided two sufficient conditions on the discrete probability distribution of the source to get shorter expected codeword length than that of Omega coding. Eventually, we applied our proposed algorithm to some first positive integers and observed its better performance compared with the codeword length for Elias ω coding scheme.

Acknowledgments

The authors would like to thank Dr. Farzan Haddadi for his valuable comments and helpful suggestions. This work has been supported in part by the Iran NSF under Grant No. 92/32575 and by the Iran Telecommunication Research Center (ITRC).

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